

# Machine Learning, Probabilistic Inference, System Identification and Control

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Carl Edward Rasmussen

Department of Engineering, University of Cambridge

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with thanks to my students:

Marc Deisenroth, Roger Frigola, Joe Hall & Andrew McHutchon

# Adaptive Systems Wish List

Good adaptive systems must be

- flexible
- automatic
- efficient
- able to handle noise and uncertainty
- practical
- optimal
- provably stable

# Adaptive Systems Wish List – Realistic Version

Good adaptive systems must be

- flexible
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# Probabilistic or Bayesian Inference

Probability theory is a framework ideally suited to make inferences under uncertainty

- able to handle noise and uncertainty
- automatic
- efficient,

but, can it be made

- flexible?
- practical?

Unfortunately, the Bayesian framework is often misunderstood.

# Be flexible: Don't Lie

Cromwell's dictum:

*I beseech you, in the bowels of Christ, think it possible that you may be mistaken*

In modeling terms

- **don't** assign zero probability to something that *might* be true  
Ex.: 'The friction is assumed purely viscous'.
- **don't** condition on things which *might not* be true.  
Ex.: 'The Kalman filter is optimal for linear Gaussian systems'.

How can we achieve this? Non-parametric inference over functions

# Learning Dynamics: Short and Long time Horizons

It is only tractable to capture *short term* dynamics . . .

. . . but you need to understand *long term* dynamics to control

⇒

- learn short term dynamics
- make probabilistic predictions (because we don't know the *exact* dynamics)
- **probabilistically** cascade predictions to get long term behaviour
- propagating a Gaussian state distribution through a non-linear dynamics model is intractable: use moment matching

# Learning Algorithm

Require:

- reward or loss function
- initial policy or control law (random)

Algorithm:

- execute current algorithm in the real world, collect data
- train the short term dynamics models on all available data
- evaluate different controllers by *simulating* their long term performance
- pick the best controller you can find (using gradient based minimization)
- repeat

# Cart and Pole

Loss function geometric (not dynamic).

Short term (100ms) dynamics are captured by 4 separate GP models.

A non-linear parameterized state feedback policy is optimized based on the experience so far.

The system learns quickly and automatically, from essentially no prior knowledge:

- relevant time frames: sampling time 100 ms, horizon 2 s.
- dynamics are smooth
- dynamics are time-invariant
- scale for the loss function

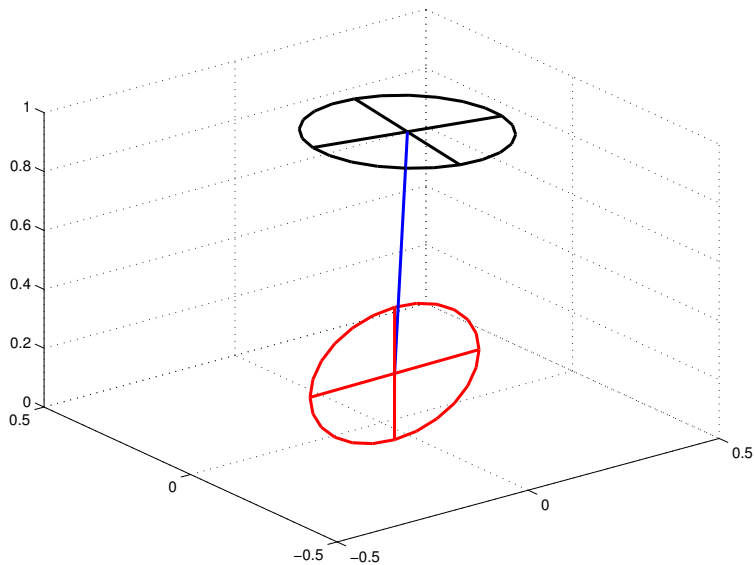


# Properties of the Solution

Some observations about the learner

- Dynamics are learnt only locally around successful trajectories
- learning algorithm is greedy
  - exploration vs exploitation
- characteristic behaviour of the uncertainty or error-bars
  - Initially, error bars are wide and expanding
  - after successful learning, error bars are collapsing

# Learning to Unicycle





# Conclusions

It is possible to learn **automatically** and **rapidly** with essentially **no prior** knowledge.

**Don't lie** about the complexity of the system: **use non-parametric models**

**Don't lie** about uncertainties: faithfully keep track of error-bars.

The learning approach is **robust** and **practical** for real applications:

- calibration of sensors and actuators unnecessary
- inaccurate assumptions unnecessary